

CLAIMS

What is claimed is:

1. A method for approximating a quadratic Bezier curve with straight edges, the curve being represented by a first anchor point, a control point, and a second anchor point, the method comprising:

- (1) pushing the first anchor point, the control point, and the second anchor point into a memory stack;
- (2) popping out the top three points in the memory stack as points a2, c, and a1;
- (3) computing a flatness F of a line formed between the points a2 and a1, wherein the flatness F is calculated as follows:

$$F(a1, c, a2) = S(a1, c, a2) / |a1a2|,$$

where S(a1, c, a2) is a triangular area formed by the points a1, c, and a2, and |a1a2| is the distance between the points a1 and a2;

- (4) determining if the flatness F is less than a threshold;
- (5) if the flatness F is less than a threshold:
 - (a) adding an edge between the points a1 and a2 to an active edge list;
 - (b) pushing the point a1 back into the memory stack.

2. The method of claim 1, further comprising:

- (6) if the flatness F is not less than a threshold:
 - (a) determining if the memory stack is full;
 - (b) if the memory stack is full:

- (i) adding an edge between the points a1 and a2 to the active edge list;
- (ii) pushing the point a1 back into the memory stack;
- (c) if the memory stack is not full, dividing the quadratic Bezier curve as follows:
 - (i) determining a midpoint c1 in a line between the points a1 and c;
 - (ii) determining a midpoint c3 in a line between the points a2 and c;
 - (iii) determining a midpoint c2 in a line between the points c1 and c3;
 - (iv) pushing the points a2, c2, c3, c1, and a2 back into the memory stack;
 - (v) looping back to step (2) and repeating the above steps.

3. The method of claim 2, further comprising calculating $S(a1, c, a2)$ as follows:

$$S(\text{divided}) = S(\text{original}) / 8,$$

wherein $S(\text{original})$ is a previous triangular area and $S(\text{divided})$ is a subsequent triangular area.

4. The method of claim 1, further comprising dividing another quadratic Bezier curve at an inflection point to form the quadratic Bezier curve.

5. A method for approximating a quadratic Bezier curve with straight edges, the quadratic Bezier curve being represented by a first anchor point p0, a control point p1, and a second anchor point p2, the method comprising:

determining a first flatness of a line formed between the first anchor point p0 and the second anchor point p2, wherein the first flatness is a first quotient of (1) a first triangular area formed by the first anchor point p0, the control point p1, and

the second anchor point p_2 divided by (2) a first distance between the first anchor point p_0 and the second anchor point p_2 ;

if the first flatness is less than a threshold, replacing the curve with an edge between the first anchor point and the second anchor point.

6. The method of claim 5, further comprising:

if the first flatness is greater than the threshold:

dividing the quadratic Bezier curve into a first portion and a second portion, wherein (1) the first curve comprises the first anchor point p_0 , a first intermediate control point $c_1(1)$, and a first intermediate anchor point $c_2(1)$, and (2) the second curve comprises the first intermediate anchor point $c_2(1)$, a second intermediate control point $p_1(1)$, and the second anchor point p_2 :

determining a second flatness of a line formed between the first intermediate anchor point $c_2(1)$ and the second anchor point p_2 , wherein the second flatness is a second quotient of (1) a second triangular area formed by the first intermediate anchor point $c_2(1)$, the second intermediate control point $p_1(1)$, and the second anchor point p_2 divided by (2) a second distance between the first intermediate anchor point $c_2(1)$ and the second anchor point p_2 ;

if the second flatness is less than the threshold, replacing the second curve with a second edge between the first intermediate anchor point $c_2(1)$ and the second anchor point p_2 .

7. The method of claim 6, wherein:

the first intermediate control point $c_1(1)$ is a midpoint in a line between the first anchor point p_0 and the control point p_1 ;

the second intermediate control point $p1(1)$ is a midpoint in a line between the second anchor point $p2$ and the control point $p1$; and

the first intermediate anchor point $c2(1)$ is a midpoint in a line between the first intermediate control point $c1(1)$ and the second intermediate control point $p1(1)$.

8. The method of claim 6, further comprising, if the second flatness is greater than the threshold:

dividing the second portion into a third portion and a fourth portion, wherein (1) the third portion comprises the first intermediate anchor point $c2(1)$, a third intermediate control point $c1(2)$, and a second intermediate anchor point $c2(2)$, and (2) the fourth portion comprises the second intermediate anchor point $c2(2)$, a fourth intermediate control point $p1(2)$, and the second anchor point $p2$:

determining a third flatness of a line formed between the second intermediate anchor point $c2(2)$ and the second anchor point $p2$, wherein the third flatness is a third quotient of (1) a third triangular area formed by the second intermediate anchor point $c2(2)$, the fourth intermediate control point $p1(2)$, and the second anchor point $p2$ divided by (2) a third distance between the second intermediate anchor point $c2(2)$ and the second anchor point $p2$;

if the third flatness is less than the threshold, replacing the third curve with a third edge between the second intermediate anchor point $c2(2)$ and the second anchor point $p2$.

9. The method of claim 8, wherein:

the third intermediate control $c1(2)$ point is a midpoint in a line between the first intermediate anchor point $c2(1)$ and the second intermediate control point $p1(1)$;

the fourth intermediate control point $p1(2)$ is a midpoint in a line between the second anchor point $p2$ and the second intermediate control point $p1(1)$; and

the second intermediate anchor point $c2(2)$ is a midpoint in a line between the third intermediate control point $c1(2)$ and the fourth intermediate control point $p1(2)$.

10. The method of claim 6, further comprising, if the second flatness is less than the threshold:

determining a third flatness of a line formed between the first intermediate anchor point $c2(1)$ and the first anchor point $p0$, wherein the third flatness is calculated as (1) a third triangular area formed by the first intermediate anchor point $c2(1)$, the first intermediate control point $c1(1)$, and the first anchor point $p0$ divided by (2) a third distance between the first intermediate anchor point $c2(1)$ and the first anchor point $p0$;

if the third flatness is less than the threshold, replacing the first curve with an edge between the first intermediate anchor point $c2(1)$ and the first anchor point $p0$.

11. The method of claim 8, further comprising calculating the second and the third triangular areas as follows:

$$S(\text{divided}) = S(\text{original}) / 8,$$

wherein $S(\text{original})$ is a previous triangular area and $S(\text{divided})$ is a subsequent triangular area.

12. The method of claim 5, further comprising dividing another quadratic Bezier curve at an inflection point to form the quadratic Bezier curve.